

Chapter 8: Comparing Quantities

- 1) Ratio is the mean of comparing quantities.
- 2) The ratio a is to $b =$ fraction $\frac{a}{b} =$ written as $a:b$
- 3) Equivalent ratio : To compare different ratios convert fractions into like fractions. If like fractions are equal, then the given ratios are said to be equivalent.
e.g. Compare $1:2$ and $2:3$

$$\frac{1}{2} = \frac{1 \times 3}{2 \times 3} = \frac{3}{6}, \quad \frac{2}{3} = \frac{2 \times 2}{3 \times 2} = \frac{4}{6}$$

$$\text{We find } \frac{3}{6} < \frac{4}{6} \therefore \frac{1}{2} < \frac{2}{3}$$

$\therefore 1:2$ is not equivalent to ratio $2:3$.

- 4) Ratio in simplest form : The ratio $(a:b)$ is said to be in simplest form, if HCF of a and b is 1. i.e. no common factor between "a" and "b" other than 1.
It is also called lowest term.

- 5) Proportions : Four quantities a, b, c and d are said to be in proportion, if $a:b = c:d$ i.e. $\frac{a}{b} = \frac{c}{d}$

- 6) Unitary method : Value of unit (one) quantity is obtained first.

e.g. Cost of 6 books = Rs. 90
Cost of 1 book = $\frac{\text{Rs. } 90}{6} = \text{Rs. } 15$

Cost of 10 books = $\text{Rs. } 15 \times 10$
= Rs. 150

7) Percentage mean per 100. (Out of 100)

$$1\% = \frac{1}{100} = 0.01 \quad 14\% = \frac{14}{100} = 0.14 \quad \text{etc.}$$

9) To convert a fraction ($\frac{a}{b}$) into percent, multiply the fraction by 100 and write % sign.

$$\frac{1}{3} = \frac{1}{3} \times 100\% = \frac{100}{3}\% = 33\frac{1}{3}\%$$

$$\therefore \frac{1}{3} = 33\frac{1}{3}\%$$

$$\frac{4}{5} = \frac{4}{5} \times 100\% = \frac{400}{5}\% = 80\%$$

10) To convert decimals into percent, shift the decimal point two (2) places to the right side and write % sign.

$$0.75 = 0.75 \times 100\% = 75\%$$

$$0.09 = 0.09 \times 100\% = 9\%$$

$$0.2 = 0.2 \times 100\% = 20\%$$

11) Converting percentage (%) to fraction or decimal.

$$75\% = \frac{75}{100} = 0.75$$

$$9\% = \frac{9}{100} = 0.09$$

$$20\% = \frac{20}{100} = 0.2$$

12) Converting percentages to "how many".

$$25\% \text{ of } 40 = \frac{25}{100} \times 40 = 10$$

'of' means \times (multiplication)

$$25\% \text{ of } P = 20 \Rightarrow \frac{25}{100} \times P = 20 \Rightarrow P = \frac{20 \times 100}{25} = 80.$$

13) Ratio to Percent (%): Given ratio 2:1 (Rice: Dal)

$2+1=3$ (Total parts) $\frac{2}{3}$ is Rice part, $\frac{1}{3}$ is Dal part.

$$\frac{2}{3} \times 100\% = \frac{200}{3}\% = 66\frac{2}{3}\%$$

$$\frac{1}{3} \times 100\% = \frac{100}{3}\% = 33\frac{1}{3}\%$$

14) Increase or decrease as percent

$$\% \text{ increase or decrease} = \frac{\text{Change in amount}}{\text{Original or base amount}} \times 100$$

e.g.

School team won 4 games last year and 6 games this year.

$$\% \text{ increase} = \frac{6-4}{4} \times 100\% = \frac{2}{4} \times 100\% = 50\%$$

15) S.P. - Selling Price C.P. - Cost Price

When $S.P. > C.P.$ then Profit = $S.P. - C.P.$

$$\text{Profit}\% = \frac{S.P. - C.P.}{C.P.} \times 100$$

When $S.P. < C.P.$ then Loss = $C.P. - S.P.$

$$\text{Loss}\% = \frac{C.P. - S.P.}{C.P.} \times 100$$

16) Simple Interest (S.I.) = $\frac{P \times R \times T}{100}$ P - Principal
R - Rate of Interest
T - Time (years)

$$\text{Amount} = \text{Principal} + \text{S.I.}$$